

## Universitas Brawijaya Faculty of Mathematics and Natural Sciences Department of Statistics / Bachelor Statistics Study Programme

| Module Handbook              |  |  |  |  |  |
|------------------------------|--|--|--|--|--|
| Module Name:                 | Matrix and Vector Spaces (MAS62113)                        |  |  |  |  |
| Module Level:                | Bachelor   |  |  |  |  |
| Abbreviation, if applicable: | -  |  |  |  |  |
| Sub-heading, if applicable:  | -  |  |  |  |  |
| Courses included in the      | -  |  |  |  |  |
| module, if applicable:       |  |  |  |  |  |
| Semester/term:               | 2nd / First Year   |  |  |  |  |
| Module Coordinator(s):       | Luthfatul Amaliana, S.Si., M.Si                            |  |  |  |  |
| Lecturer(s):                 | 1. Dr. Ir. Bernadetha Theresia Mitakda                     |  |  |  |  |
|                              | 2. Luth  | fatul Amaliana, S.Si., M.Si.   |  |  |  |
|                              | 3. Dr. 5   | <ul><li>3. Dr. Suci Astutik, M.Si.</li><li>4. Nur Silviyah Rahmi, S.Si., M.Stat</li></ul>  |  |  |  |
|                              | 4. Nur   |  |  |  |  |
| Language:                    | Indonesian   |  |  |  |  |
| Classification within the    | Compulsory course  |  |  |  |  |
| curriculum:                  |  |  |  |  |  |
| Teaching format / class per  | $3 \times 50$ minutes                                      |  |  |  |  |
| week during semester:        |  |  |  |  |  |
| Workload:                    | 2.5 hours lectures, 3 hours structural activities, 3 hours |  |  |  |  |
|                              |  | ual studies, 16 weeks per semester, and total 136 hours  |  |  |  |
|                              | per semester 4.5 ECTS                                      |  |  |  |  |
| Credit Points:               | 3  |  |  |  |  |
| Requirements:                | Mathematics (MAS61111)                                     |  |  |  |  |
| Learning goals /             | General Competence (Knowledge):                            |  |  |  |  |
| competencies:                | ILO1   | The students are able to master basic scientific<br>concepts and statistical analysis methods applied on<br>computing, social science, humanities, economics,<br>industry and life science.  |  |  |  |
|                              | ILO5   | The students are able to apply logical, critical,<br>systematic, and innovative thinking independently<br>when applied to science and technology that contain<br>humanities values, based on scientific principles,<br>procedures and ethics with excellent and measurable<br>results. |  |  |  |
|                              | ILO6   | The students are able to take appropriate decisions to<br>solve the problems expertly, based on the information<br>and data analysis.  |  |  |  |

|           | ILO8    | The students are able to apply and internalize the  |  |  |
|-----------|---------|---|--|--|
|           |         | The students are able to apply and internalize the spirit of independence, struggle, entrepreneurship |  |  |
|           |         | spirit of independence, struggle, entrepreneurship,   |  |  |
|           |         | based on values, norms, and academic ethics of  |  |  |
|           | G • • • | Pancasila in all aspects of life.   |  |  |
|           |         | Specific Competence:  |  |  |
|           | M1      | Students are able to explain the concept of Linear  |  |  |
|           |         | Equation System (LES) and can find the solutions.   |  |  |
|           |         | (ILO1, ILO5, ILO6, ILO8)  |  |  |
|           | M2      | Students are able to explain the concept of matrix. (ILO1, ILO5, ILO6, ILO8)                          |  |  |
|           |         |   |  |  |
|           | M3      | Students are able to explain the determinant and  |  |  |
|           |         | inverse matrix. (ILO1, ILO5, ILO6, ILO8)  |  |  |
|           | M4      | Students are able to explain vectors in Space-2 and   |  |  |
|           |         | Space-3. (ILO1, ILO5, ILO6, ILO8)   |  |  |
|           | M5      | Students are able to explain the concept of Vector<br>Spaces. (ILO1, ILO5, ILO6, ILO8)                |  |  |
|           |         |   |  |  |
|           | M6      | Students are able to explain Linear Transformation.   |  |  |
|           |         | (ILO1, ILO5, ILO6, ILO8)  |  |  |
|           | M7      | Students are able to explain Eigen Values, Eigen  |  |  |
|           |         | Vectors, and applications in matrix diagonalization.  |  |  |
|           |         | (ILO1, ILO5, ILO6, ILO8)  |  |  |
|           | M8      | Students are able to do Singular Value Decomposition (SVD) and Quadratic Form. (ILO1, ILO5, ILO6,     |  |  |
|           |         |   |  |  |
|           |         | ILO8)   |  |  |
| Contents: | 1       | LES, Gauss elimination, Gauss-Jordan elimination,   |  |  |
|           |         | homogeneous LES.  |  |  |
|           | 2       | Matrix and matrix operations, elementary matrix,  |  |  |
|           |         | transpose matrix, inverse matrix, diagonal matrix,  |  |  |
|           |         | triangular matrix, matrix partition, general inverse  |  |  |
|           |         | matrix, Kronecker matrix.   |  |  |
|           | 3       | Determinant Functions, Determine Determinants   |  |  |
|           |         | using Row Reduction, Determinant Function   |  |  |
|           |         | Properties, Co-factor Expansion, Minor Co-factors,  |  |  |
|           |         | Cramer Rules.   |  |  |
|           | 4       | Vectors in Space-2 and Space-3: norms, vector   |  |  |
|           |         | arithmetic, dot product, projection, cross product, line  |  |  |
|           |         | and plane in Space-3.   |  |  |
|           | 5       | Euclidis n-space, general vector space, linear  |  |  |
|           | _       | independence, basis and dimensions, rank, inner   |  |  |
|           |         | product space, orthonormal basis, Gram-Schmidt  |  |  |
|           |         | process.  |  |  |
|           |         | P   |  |  |

|                         | 6 Linear transformations, pro  | nantiag of linear                                    |  |
|-------------------------|--|--|--|
|                         |  |  |  |
|                         |  | transformations, linear transformations from Space-n |  |
|                         | to Space-m, linear transform   |  |  |
|                         | 7 Eigenvalue, eigenvector, di  | • •  |  |
|                         | and orthonormal diagonaliz   | ation, symmetric matrix.                             |  |
|                         | 8 Singular Value Decomposit  | tion (SVD), Quadratic                                |  |
|                         | form.  |  |  |
| Soft skill attribute:   | Responsible, independently, and discipline   |  |  |
| Study/exam achievement: | Final score (NA) is calculated as follow: 15% Assignments,   |  |  |
|                         | 20% Quizzes, 10% Tutorial Class, 25% Midterm Test, 25%   |  |  |
|                         | Final Exam, 5% Attitude  |  |  |
|                         | Final index is defined as follow:<br>A :> 80 - 100   |  |  |
|                         |  |  |  |
|                         | B+ :> 75 - 80  |  |  |
|                         | B :> 69 - 75   |  |  |
|                         | C+ :> 60 - 69  |  |  |
|                         | C :> 55 - 60   |  |  |
|                         | D+ :> 50 - 55  |  |  |
|                         | D = 250 - 50<br>D = 200 - 50   |  |  |
|                         |  |  |  |
| Forms of media:         | E : 0 - 44<br>Laptop, LCD projector, whiteboard  |  |  |
|                         |  |  |  |
| Learning methods:       | Lecture, assessments, and discussion<br>Main:  |  |  |
| Literature:             |  |  |  |
|                         | <ol> <li>Anton, H dan Rorres, C. 2013. Elementary Linear Algebra<br/>with Applications. Ninth Edition. John Wiley and Sons, Inc.</li> <li>Anton, H. 1995. Aljabar Linear Elementer. Edisi Kelima.</li> </ol> |  |  |
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|                         |  |  |  |
|                         | Alih Bahasa: Silaban, P. dan Susila, I. N. Penerbit Erlangga,  |  |  |
|                         | Jakarta.   |  |  |
|                         | Support:   |  |  |
|                         | I. Nasoetion, A. H. 1980. Aljabar N  | latriks. Penerbit Bhratara                           |  |
|                         | Karya Aksara Jakarta.  |  |  |
|                         | 2. Lipschutz, S. dan Lipson, M.L. 2009. Linear Algebra,  |  |  |
|                         | Schaum's Outlines. Fourth Edition. The McGraw-Hill   |  |  |
|                         | Companies, Inc.  |  |  |
|                         | 3. Schott, J. R. 2017. Matrix Analysis for Statistics. Third   |  |  |
|                         | Edition. John Wiley and Sons, Inc.   |  |  |
|                         | 4. Searle, S. R. dan Khuri, A. I. 2017. Matrix Algebra Useful  |  |  |
|                         | for Statistics. Second Edition. John   | Wiley and Sons, Inc.                                 |  |
| Notes:                  |  |  |  |
|                         |  |  |  |